

# Deep Learning for Rainfall-Runoff Modeling

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`neuralhydrology.github.io`

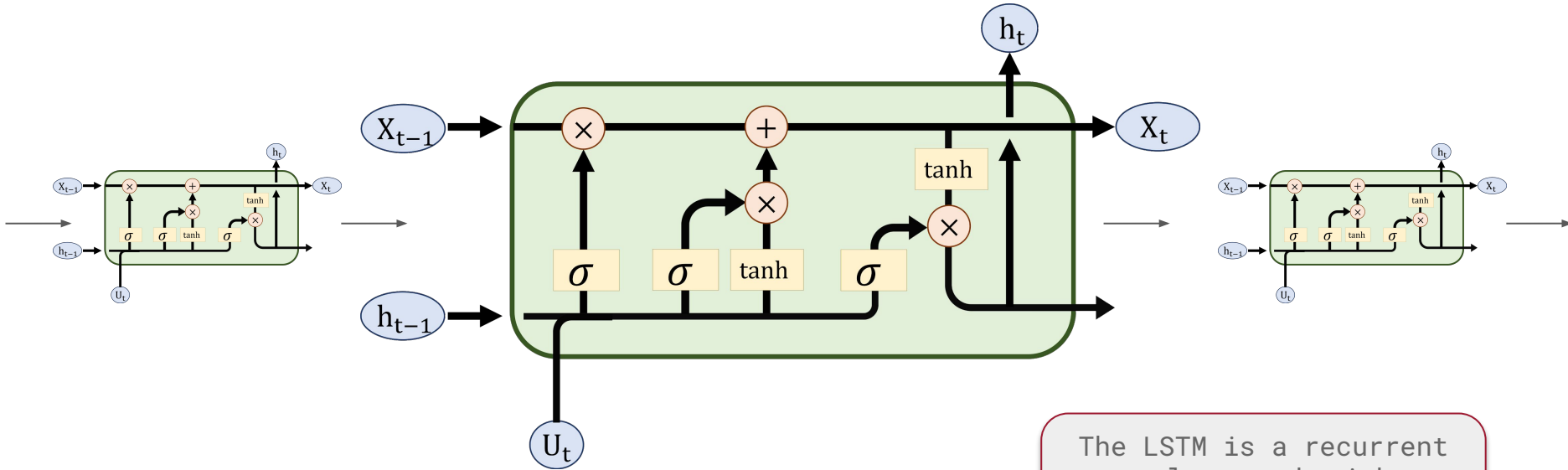
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Tech, Public Benefit Corporation, <sup>5</sup>NASA Center for Climate Simulation, <sup>6</sup>Instituto de Hidraulica Ambiental de la  
Universidad de Cantabria, <sup>7</sup>University of Arizona

# Long Short Term Memory (LSTM)



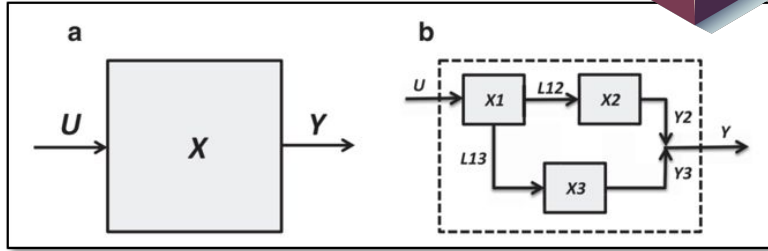
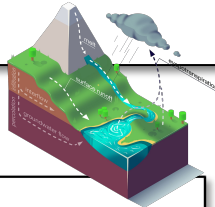
The LSTM is a recurrent neural network with an input-output-state relationship.

# LSTMs are State-Space Models

## State space model:

$$\mathbf{S}[t] = f(\mathbf{I}[t], \mathbf{S}[t-1]; \Theta_i)$$

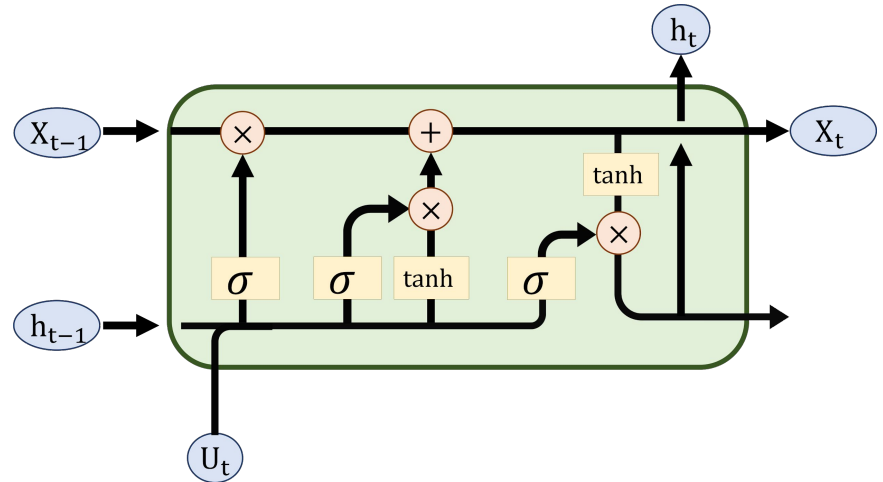
$$\mathbf{O}[t] = g(\mathbf{S}[t]; \Theta_j)$$



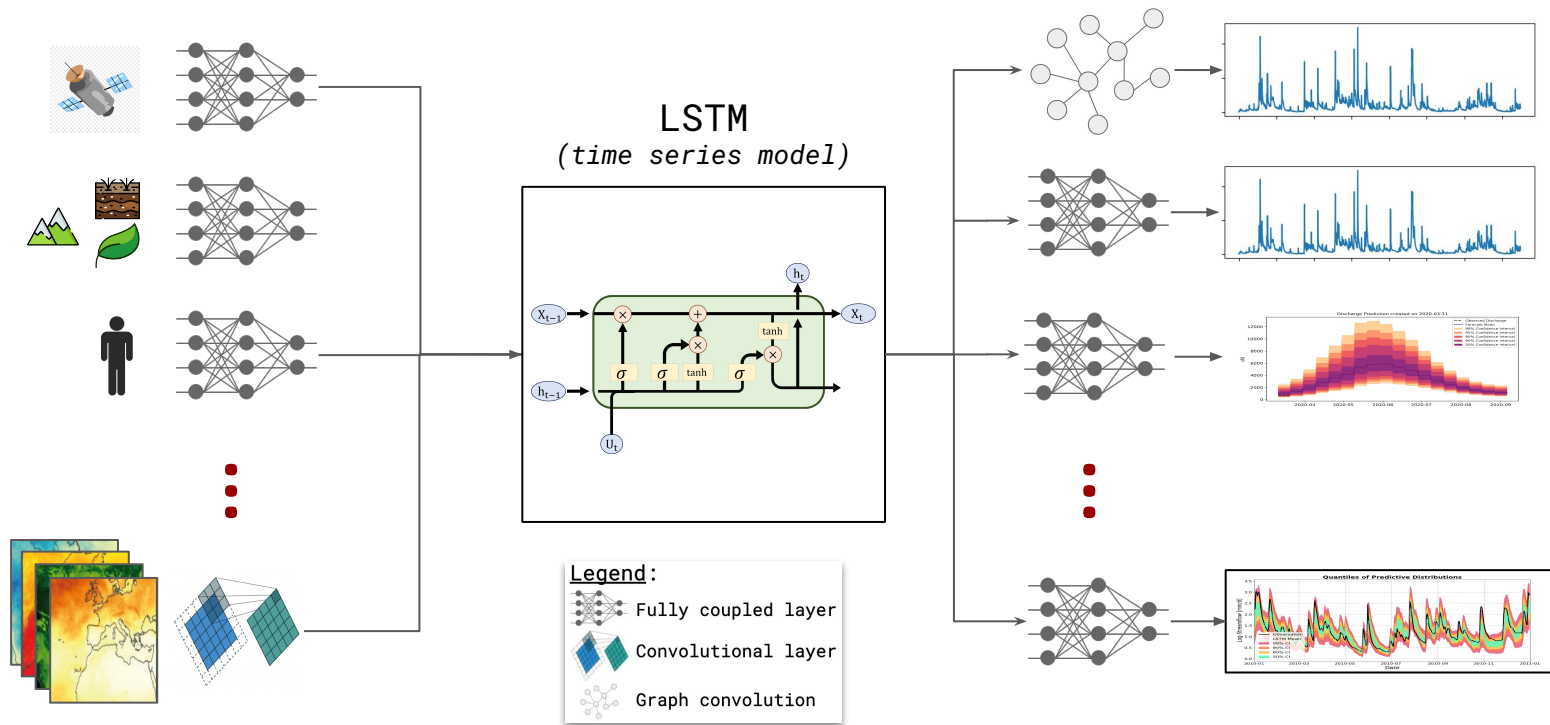
## LSTM model:

$$\{\mathbf{c}[t], \mathbf{h}[t]\} = f(\mathbf{x}[t], \mathbf{c}[t-1], \mathbf{h}[t-1]; \theta_i)$$

$$\hat{\mathbf{y}}[t] = g(\mathbf{h}[t]; \theta_j)$$

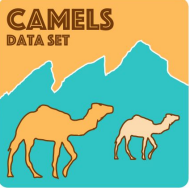


# Embedding into Deep Learning Models

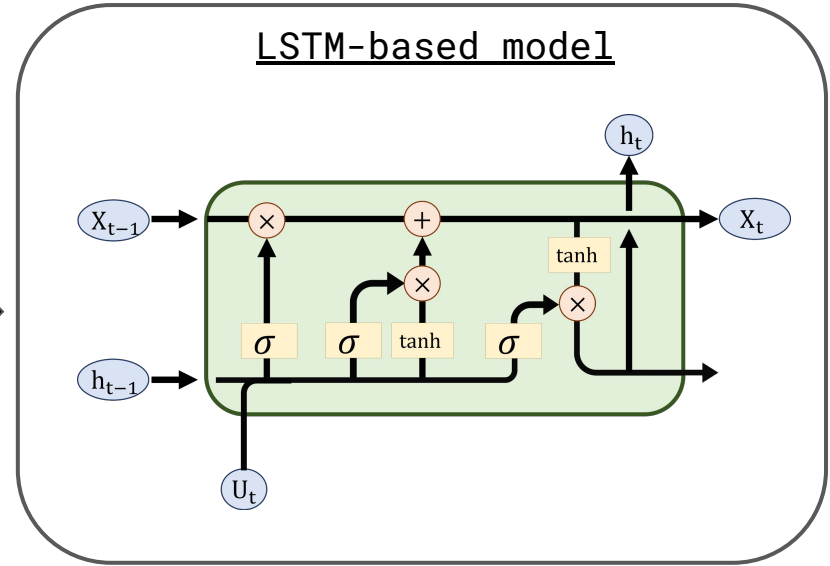
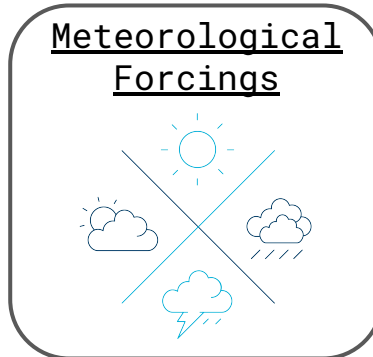
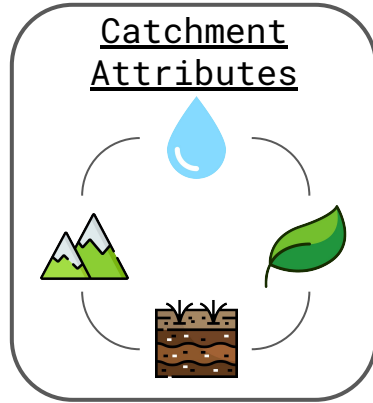


# Experimental Setup

531  
Basins

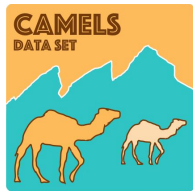
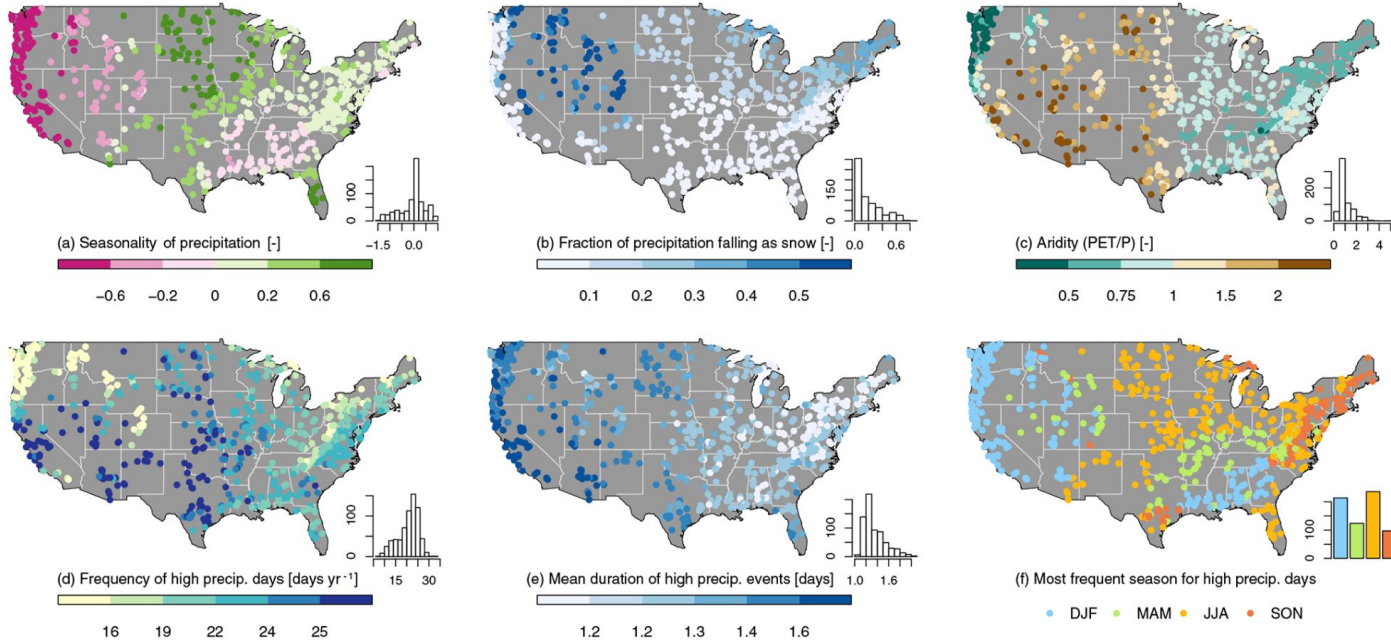


9 Years  
Training  
Data



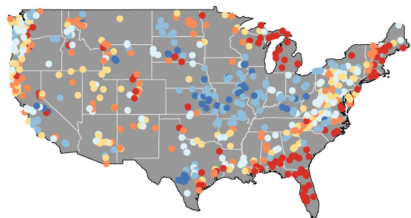
# CAMELS Dataset

531 CONUS catchments with diverse climate, ecology, geology.



Addor, N., Newman, A.J., Mizukami, N., & Clark, M.P. (2017). The CAMELS data set: catchment attributes and meteorology for large-sample studies. *Hydrology and Earth System Sciences*

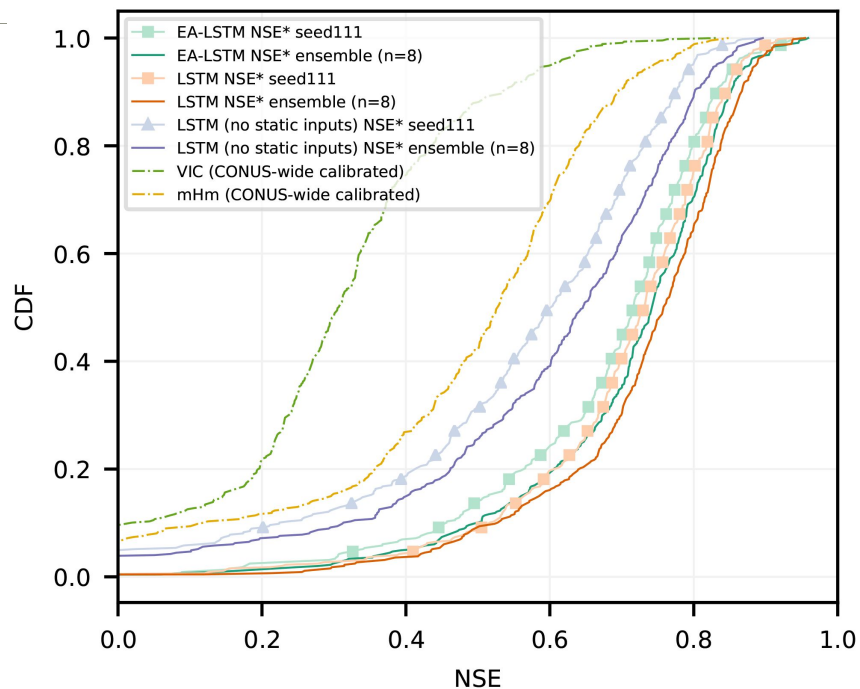
Newman, Andrew, et al. "Development of a large-sample watershed-scale hydrometeorological data set for the contiguous USA: data set characteristics and assessment of regional variability in hydrologic model performance." *Hydrology and Earth System Sciences*



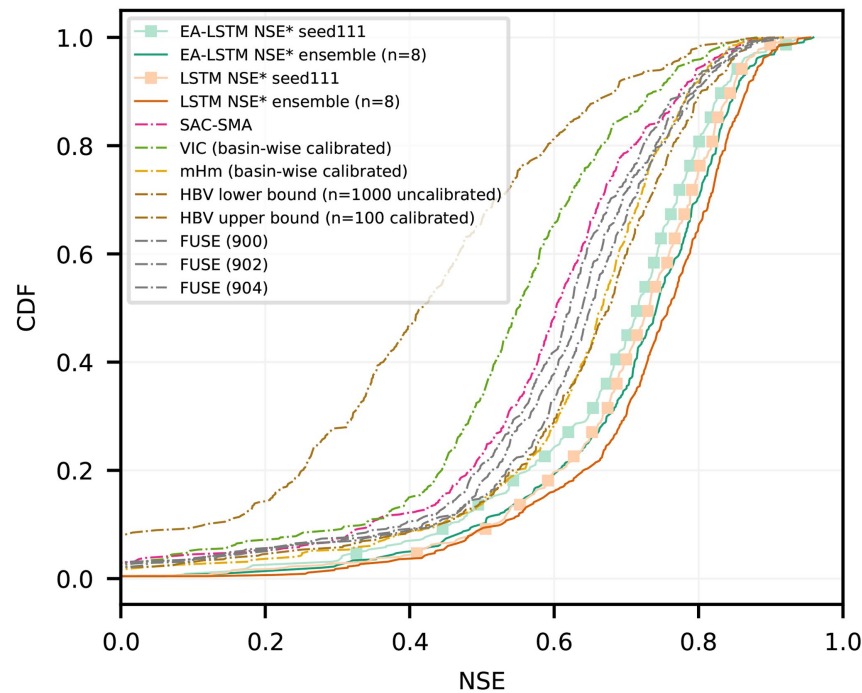
# Regional Modeling

Regional LSTMs are better than catchment-specific hydro models.

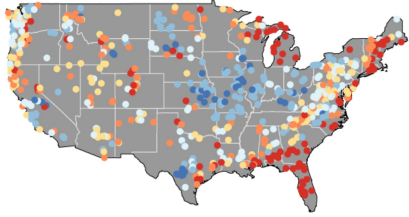
Benchmarking vs CONUS-wide calibrated models



Benchmarking vs. basin-wise calibrated models

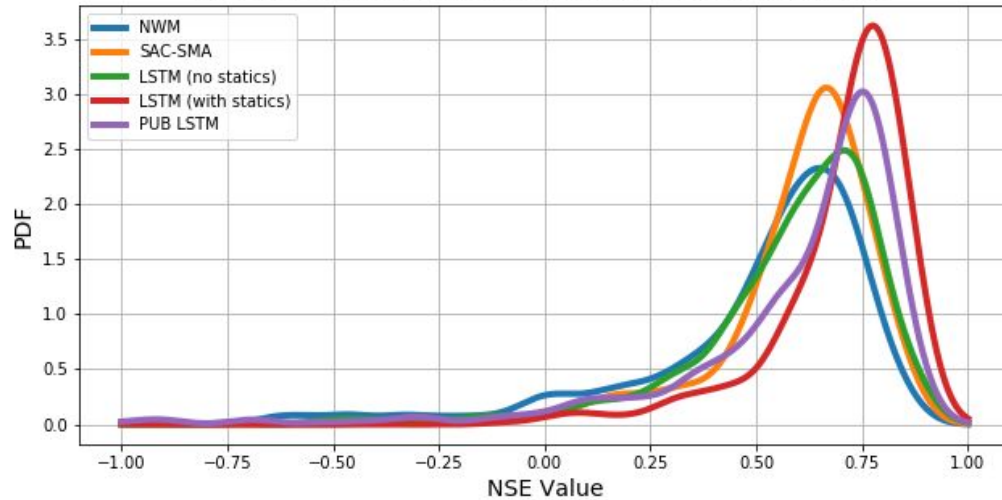


# Prediction in Ungauged Basins

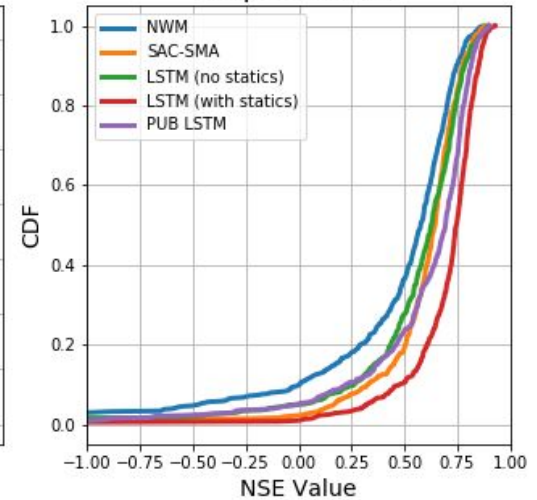


LSTMs are better in ungauged basins than SAC-SMA is in gauged basins.

Kernel Densities of NSE Values over 531 Basins

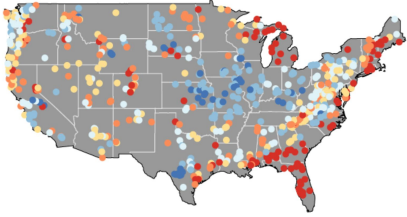


Empirical CDF

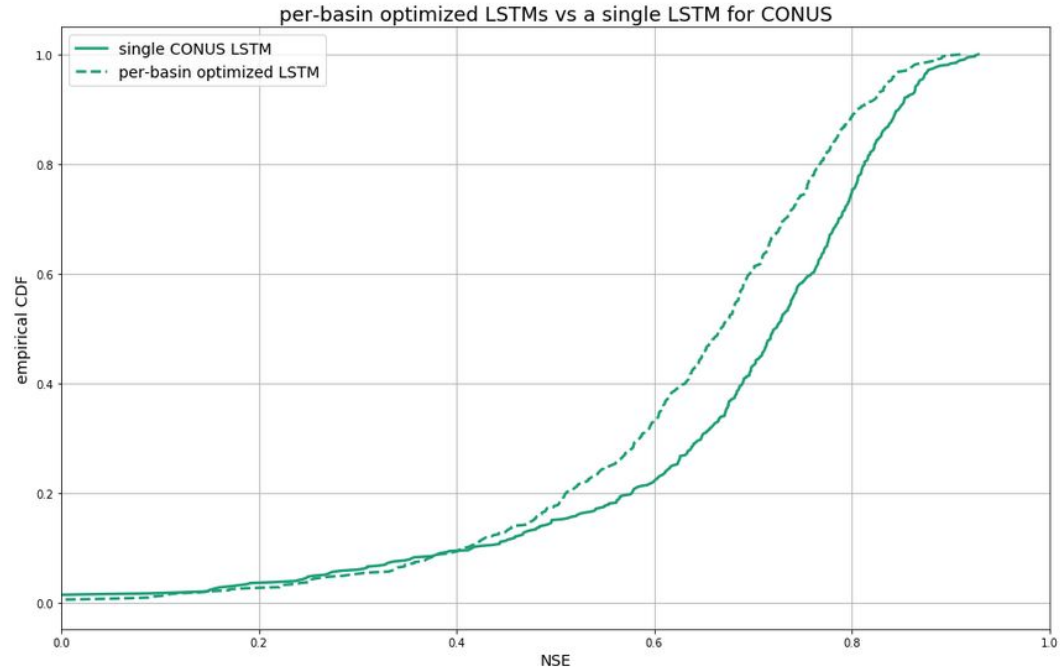




# Learning a General Model

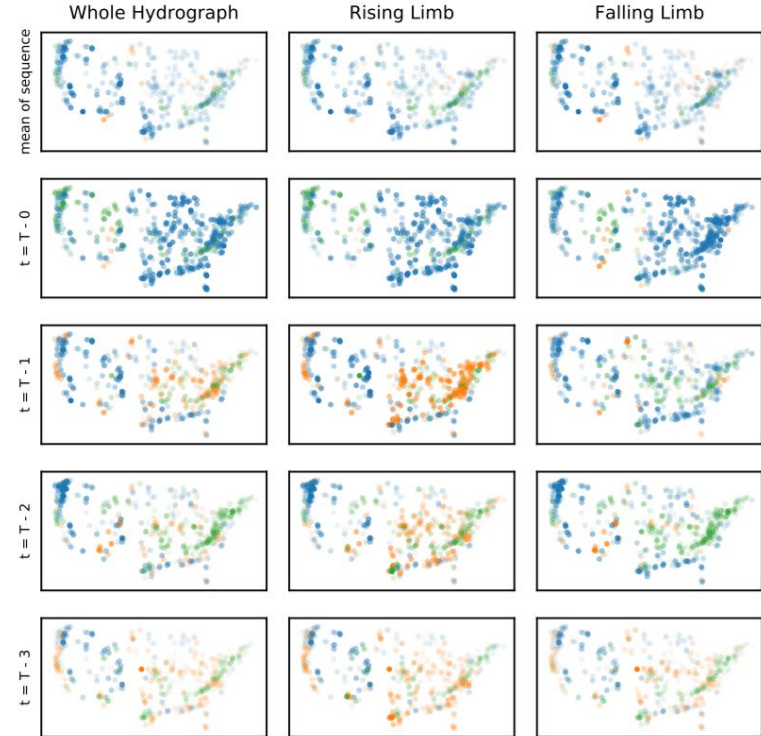
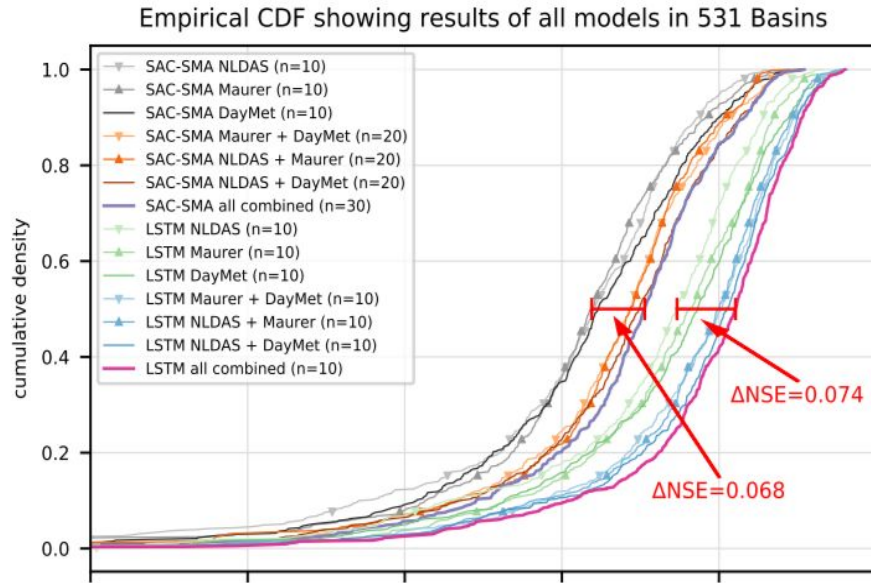


The LSTM is better when trained on multiple catchments than when trained on individual catchments.



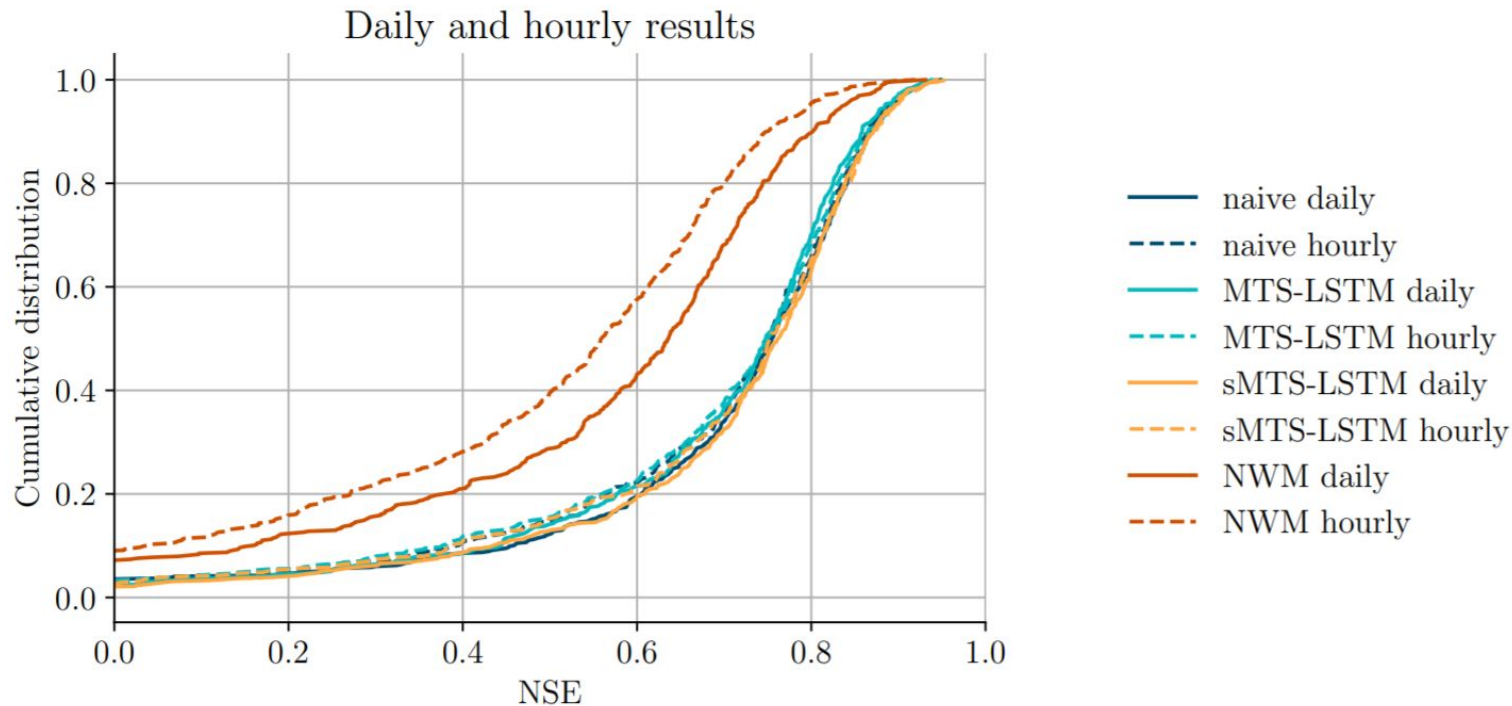
# Certain “hard” tasks are easy with DL

## Multiple Forcings w/o Ensembles



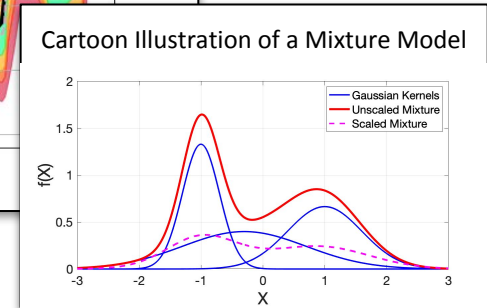
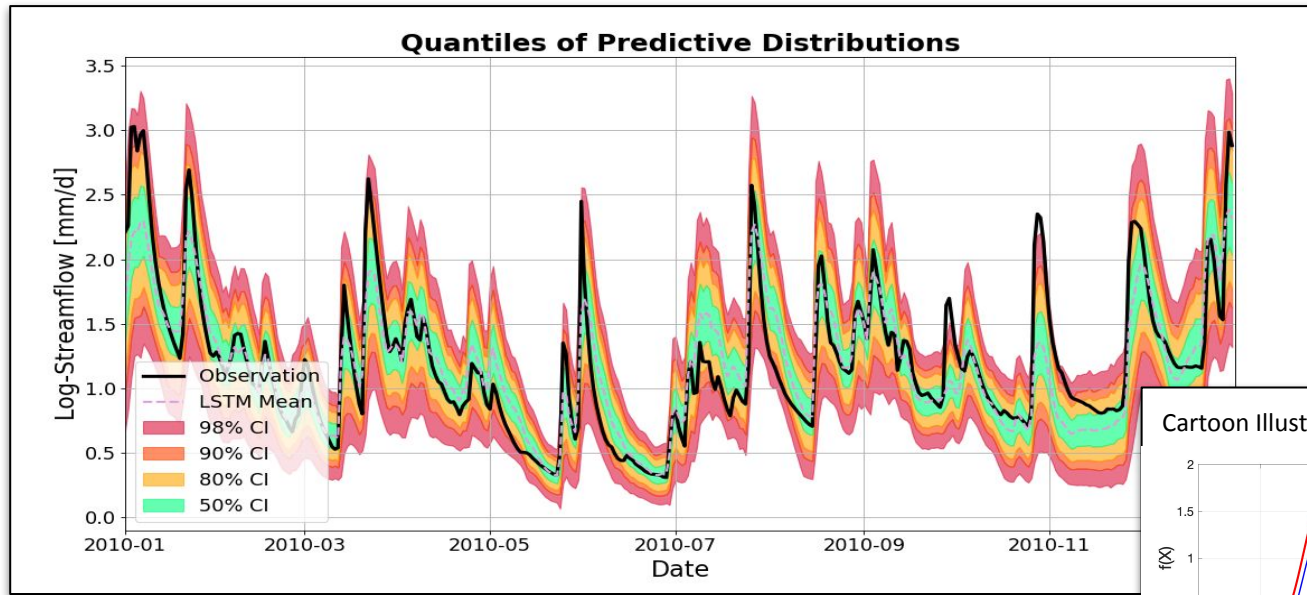
# Certain “hard” tasks are easy with DL

## Multiple Time Scales



# Certain “hard” tasks are easy with DL

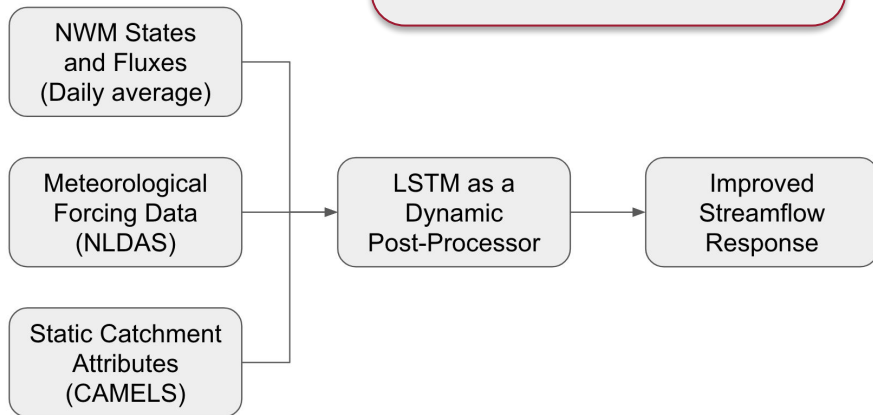
## Estimating Uncertainty



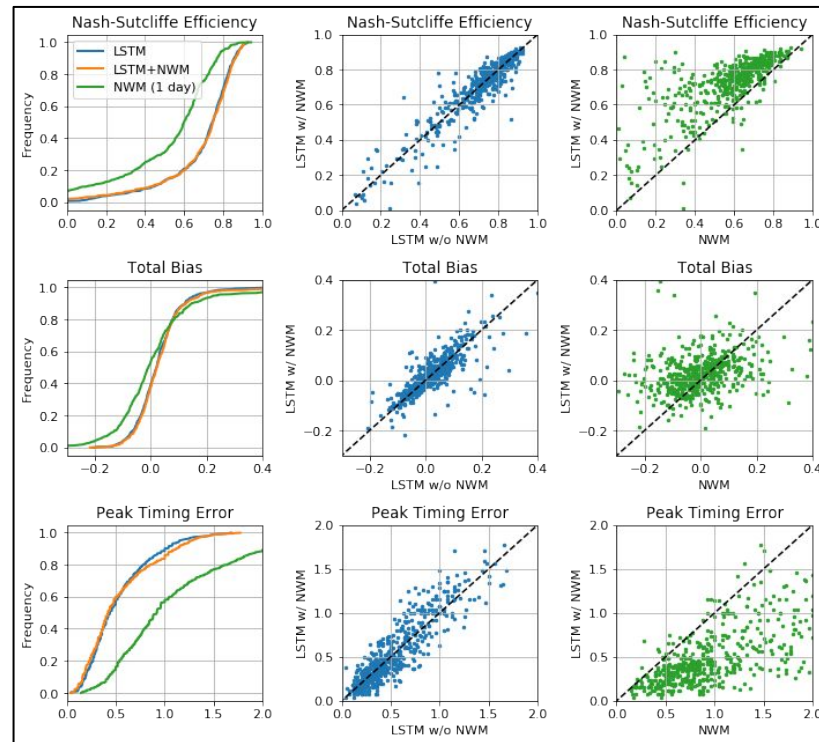
# Physics Integration

# Post-Processing

Adding NWM states and fluxes as inputs did not improve the LSTM



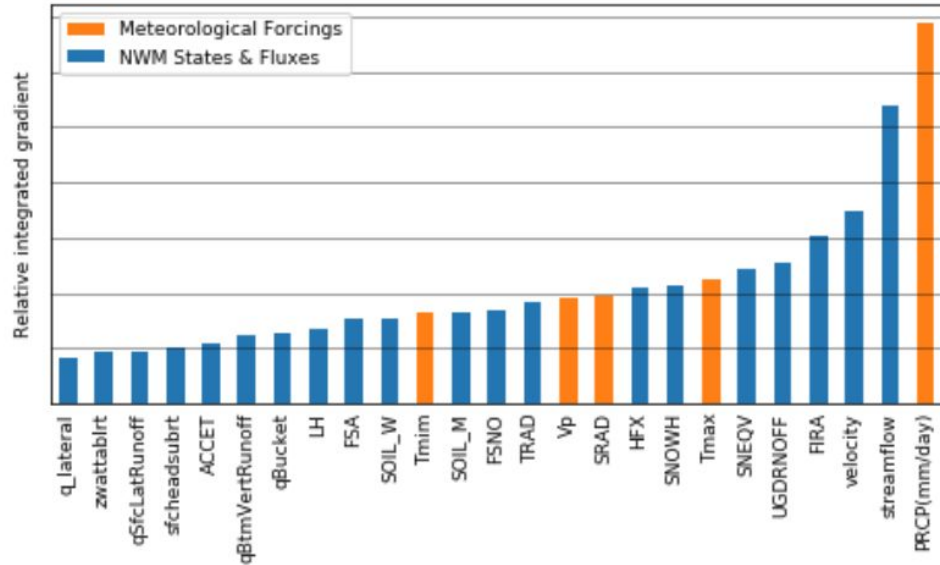
## National Water Model Post-Processing



# Post-Processing

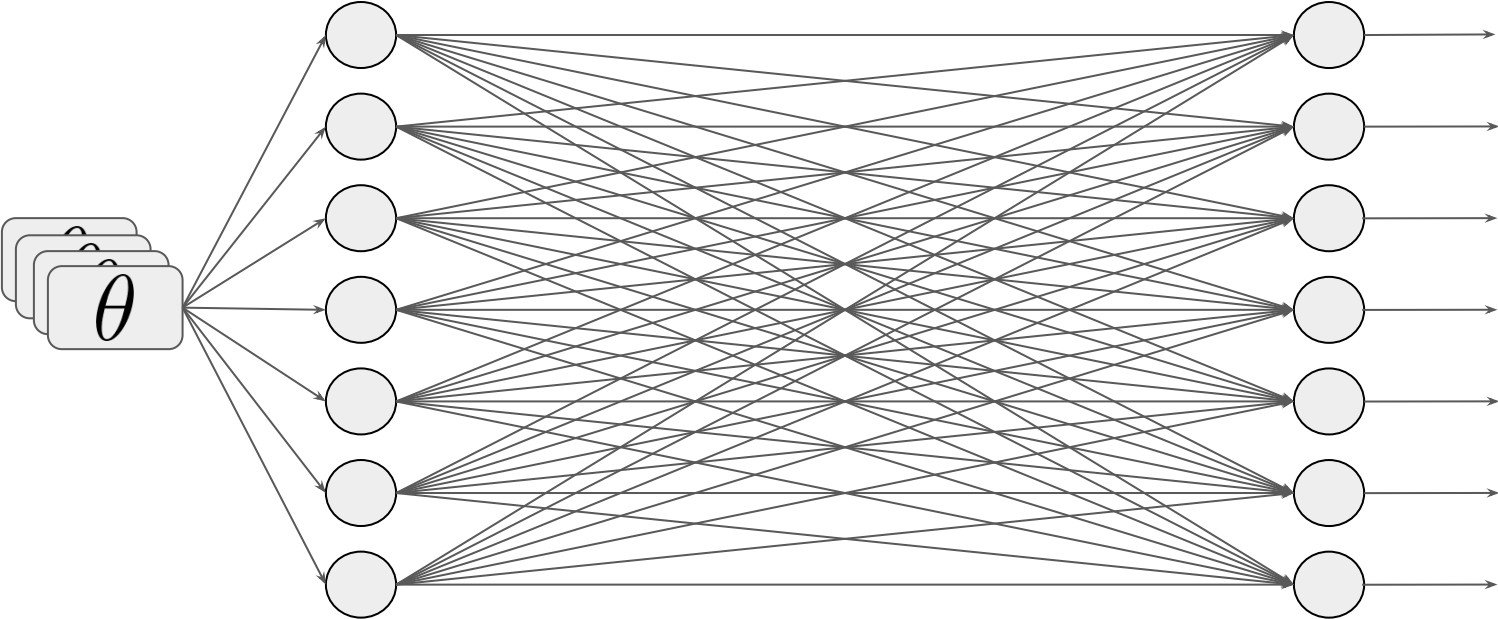
The LSTM “listens” to the NWM, but there isn’t any extra information.

## Sensitivity of LSTM to Different Inputs



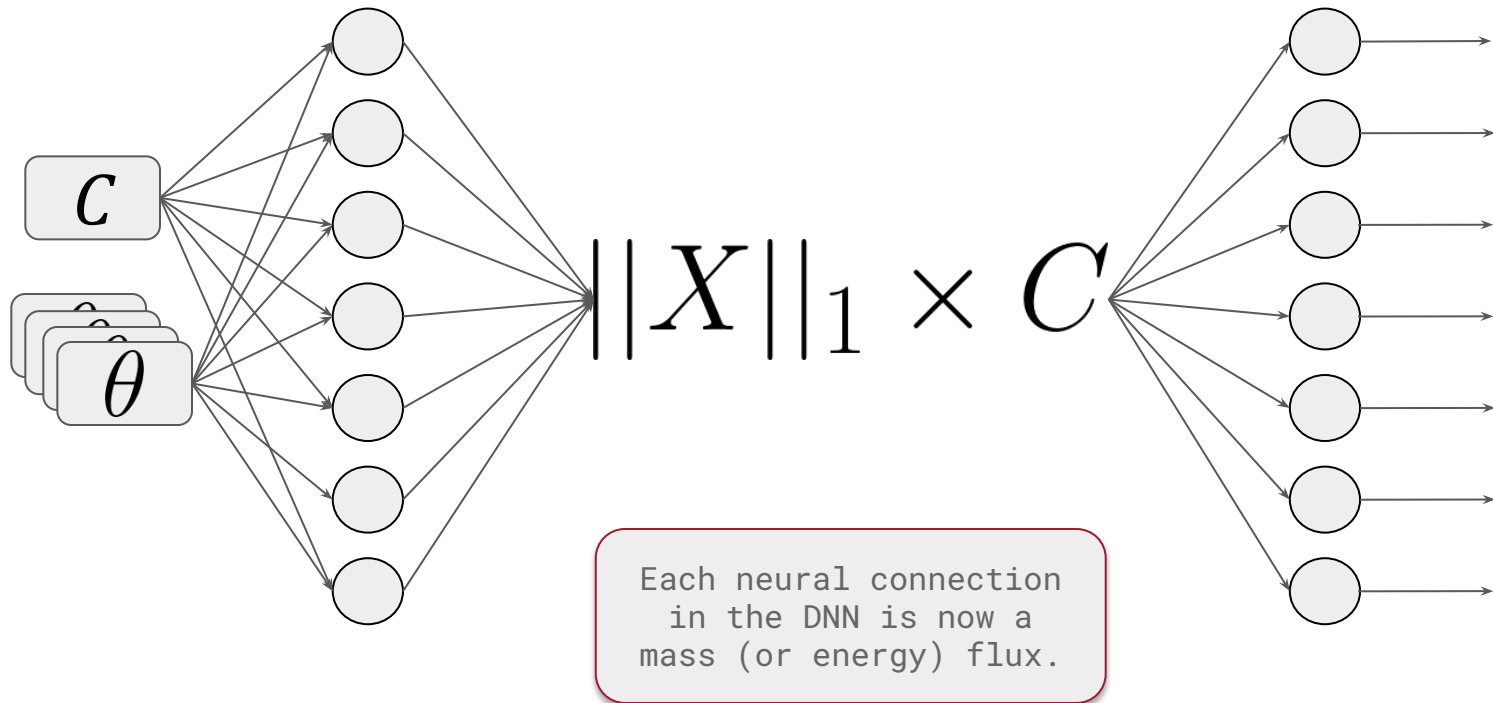
**Figure 7.** Attributions to the LSTM post-processor predictions. The vertical axis shows the relative magnitude of attribution (importance) for each input, with precipitation (PRCP) as the top contributor and NWM-predicted runoff into channel reach (q\_lateral) contributing the least.

# Physics into Deep Learning Models

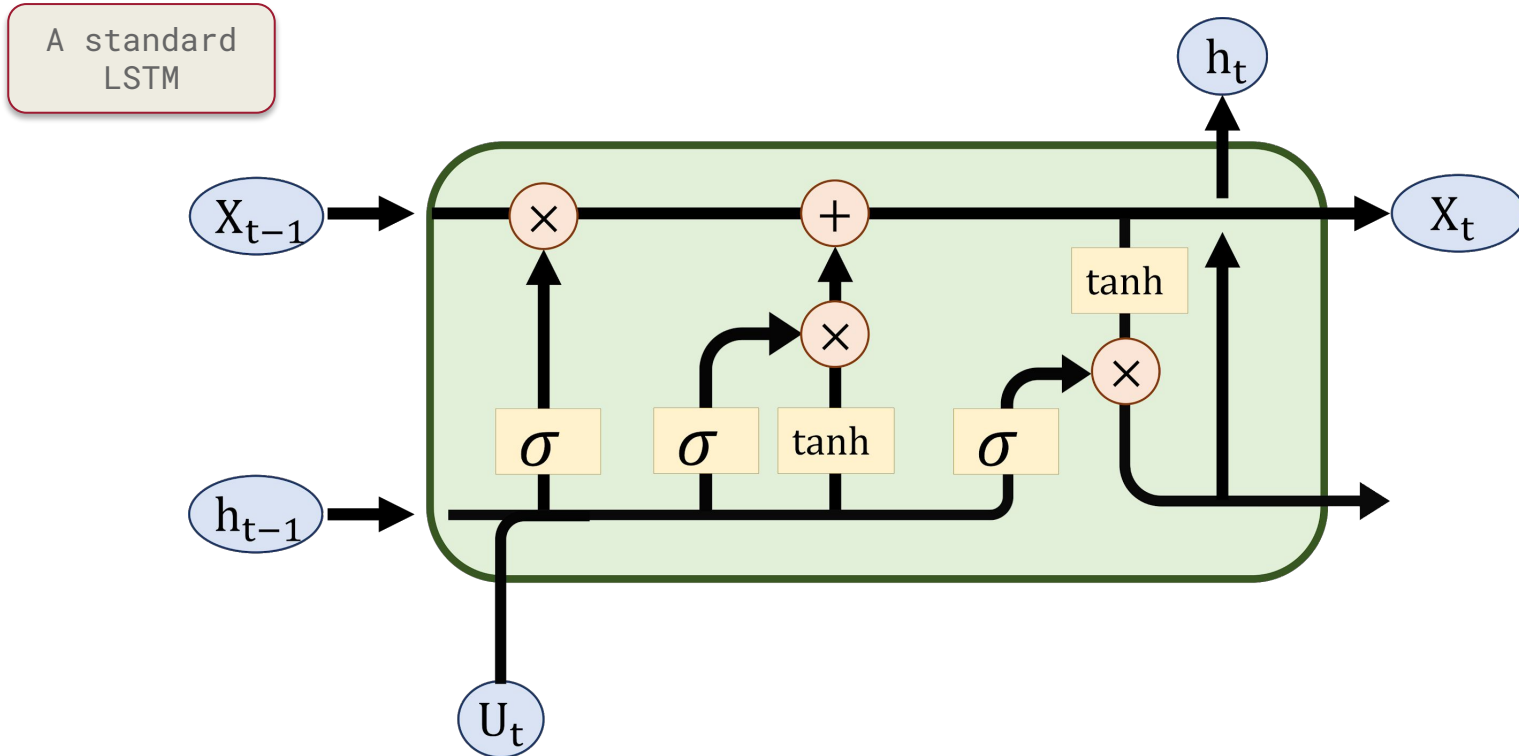




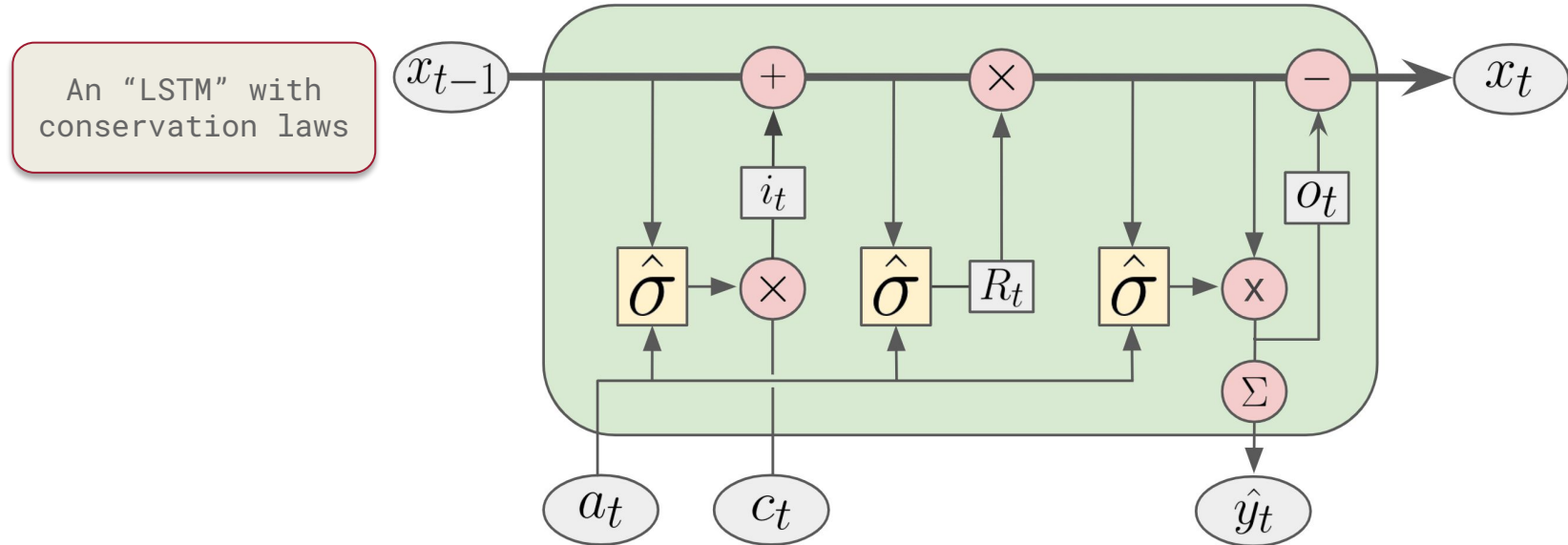
# Physics into Deep Learning Models



# Physics into Deep Learning Models



# Physics into Deep Learning Models



$$\vec{x}_t = \vec{x}_{t-1} + \dot{i}_t - \vec{o}_t$$

# Physics into Deep Learning Models

Table 1: Benchmarking Results. All values represent the median over the 447 basins.

Model	MC? <sup>a</sup>	KGE <sup>b</sup>	Bias <sup>c</sup>	$\sigma_{rat}$ <sup>d</sup>	$r^2$	FHV <sup>e</sup>	FLV <sup>f</sup>
<b>Deep Learning Models</b>							
MC-LSTM Ens.	yes	0.764*	-0.020*	0.842	0.873*	-14.689*	-24.651*
LSTM Ens.	no	0.762	-0.034	0.838	0.886	-15.740	36.267
<b>Conceptual Hydrology Models</b>							
SAC-SMA	yes	0.632	-0.066	0.779	0.792	-20.356	37.415
VIC (basin)	yes	0.588	-0.018	0.725	0.760	-28.139	-74.769
VIC (regional)	yes	0.257	-0.074	0.457	0.651	-56.483	18.867
mHM (basin)	yes	0.691	-0.040	0.807	0.832	-18.640	11.433
mHM (regional)	yes	0.468	-0.039	0.589	0.793	-40.178	36.795
HBV (lower)	yes	0.391	-0.023	0.584	0.713	-41.859	23.883
HBV (upper)	yes	0.681	-0.012	0.788	0.833	-18.491	18.341
FUSE (900)	yes	0.668	-0.031	0.796	0.815	-18.935	-10.538
FUSE (902)	yes	0.690	-0.047	0.802	0.821	-19.360	-68.224
FUSE (904)	yes	0.644	-0.067	0.783	0.808	-21.407	-67.602

<sup>a</sup>Mass conservation (MC).

<sup>b</sup>Kling-Gupta Efficiency:  $(-\infty, 1]$ , values closer to one are desirable.

<sup>c</sup>Bias:  $(-\infty, \infty)$ , values closer to zero are desirable.

<sup>d</sup>Variance Ratio:  $(-\infty, \infty)$ , values closer to one are desirable.

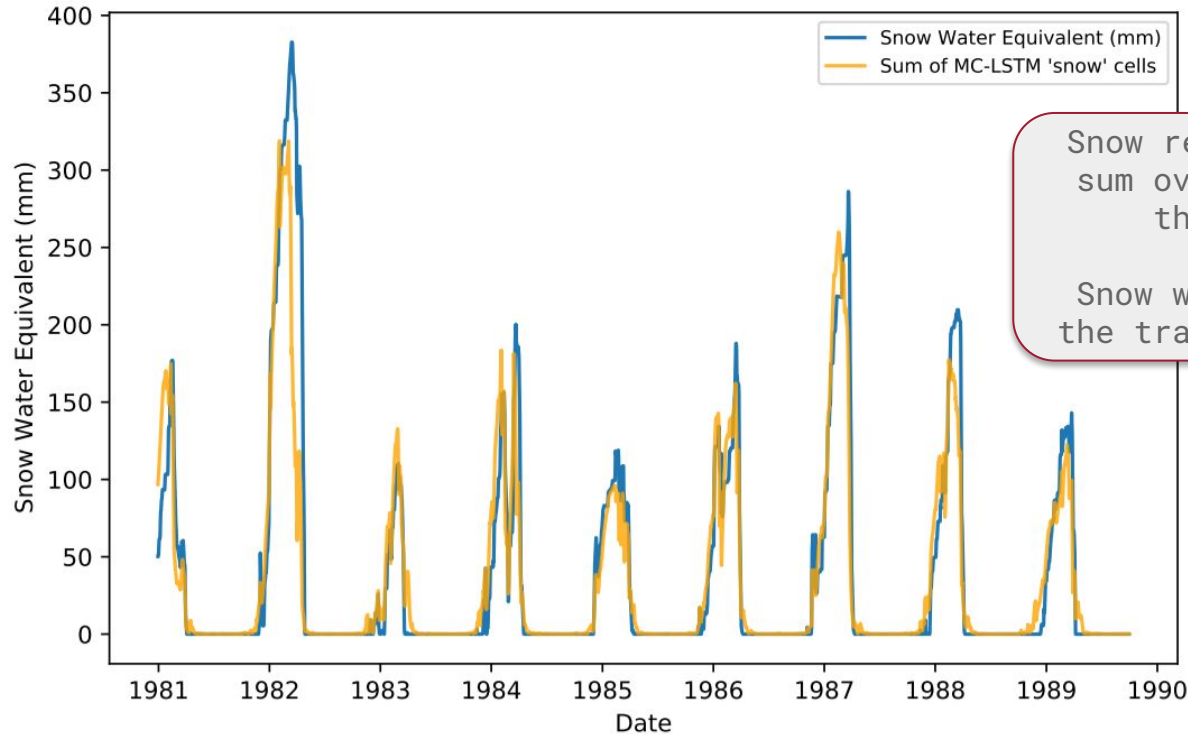
<sup>e</sup>Top 2% high flow bias:  $(-\infty, \infty)$ , values closer to zero are desirable.

<sup>f</sup>Bottom 30% low flow bias:  $(-\infty, \infty)$ , values closer to zero are desirable.

\*MC-LSTM is significantly different than the LSTM by Wilcoxon rank test at  $\alpha = 0.05$ .

Slight performance increase over LSTM, but currently the best peak-flow model we've tested.

# Physics into Deep Learning Models



Snow represented as a sum over 4 states in the MC-LSTM.

Snow was not part of the training data set.

# Contributors



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